DEM Analysis of Backfilled Walls Subjected to Active Translation Mode

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ABSTRACT

In this paper, the problem of a retaining wall under active translation mode was numerically investigated. A series of numerical models was conducted using the discrete element code, PFC2D. The backfill soil was simulated by an assembly of separate cohesionless circular particles. Backfill soil was prepared by pouring soil particles from a specific height under gravity force and giving them enough time for appropriate settlement. Different heights of retaining walls were simulated and the lateral earth pressure on the wall was observed under both at-rest and active conditions. Numerical results were compared with predictions from several analytical methods and measurements from physical models. The active state of earth pressure was defined as the earth pressure distribution corresponding to the values of wall displacement where the failure zone in the backfill was fully developed. The numerical results showed that the fully active state of earth pressure occurred at a wall displacement corresponding to the strains required for reaching the critical state in biaxial compressive tests.

Keywords: Numerical analysis, Retaining walls, Lateral earth pressure, PFC2D

1. Introduction

Retaining walls are constructed for various engineering problems, especially for civil and mining projects. Some very common types of projects which retaining walls are constructed are foundation pits, hydraulic structures, highways and railways. There is a soil-structure interaction between the retained soil and retaining structure which is one of the main concerns of geotechnical engineers who design such structures. The value and distribution of the lateral pressure exerted by retained soil or backfill against the retaining structure is very important and has been the subject of many researches. The earliest formulations of lateral earth pressure were conducted by Coulomb [1] and Rankine [2]. On one hand, Coulomb developed an upper-bound solution by considering the soil wedge between the retaining wall and the slip line under the limit equilibrium. On the other hand, Rankine developed a lower-bound solution by considering the plastic state of stress for a soil retained by a vertical and perfectly rough wall using the concept of Mohr circle. It is noticeable that those classical theories have resulted in a linear lateral earth pressure distribution on the wall. However, it was later shown that the distribution of lateral earth pressure on a retaining wall can be non-linear depending on many parameters such as the mode of wall movement, density of backfill soil and soil-wall interface friction angle [3-9].

The theory of arching in granular materials is attributed to Janssen [10] who defined it initially as the silo effect. This theory is later extended to earth ditches and buried structures [11-13], hoppers and bunkers [14-15], slopes [16-19] and retaining walls [20-24].

Terzaghi [12] addressed that the lateral earth pressure does not reach the maximum value at the toe of the wall, but at some higher levels, and he defined the concept of soil arching behind the retaining walls. He introduced the soil arching as the ability of soil particles to transfer earth pressures from yielding to stable portions.

Tsagareli [25] conducted a series of large scale instrumented physical models for a rigid retaining wall under active translation mode. He concluded that the slip surface behind the wall was independent of the wall height, and therefore, the lateral earth pressure distribution on the wall was non-linear.

Sherif and Fang [26] employed a shaking table to study the dynamic earth pressures on retaining walls rotating about the top. The results showed that the distribution of the dynamic active lateral earth pressure on the wall was non-linear and reduced to zero at the base of the wall.

Fang and Ishibashi [3] studied the lateral active earth pressure on a retaining wall model for different modes of wall movements including rotation about the top, rotation about the toe and translation. They concluded that the stress distribution on the wall was non-linear and its pattern to depend on the wall movement mode and the soil density. Therefore, the magnitude of the total thrust on the wall and the point of its application differ from those predicted by classical theories.

Niedostatkiewicz et al. [27] experimentally investigated the evolution of shear bands in cohesionless backfill sand behind retaining walls. They performed a small scale laboratory setup for active and passive cases of a rigid retaining wall subjected to different modes of movement. They concluded that the arrangement of shear zone patterns behind the wall mainly depended on the type of wall movement and the thickness of shear zone on the initial void ratio of backfill sand.

The effect of soil arching on the lateral earth pressure behind rigid retaining walls was investigated initially by Handy [20]. Later, many...
other formulations were developed attempting to improve the formulation of Handy [21-23]. In most of those formulations, a differential flat element was assumed between the wall and the Coulomb slip line to investigate a one-dimensional system of equilibrium. Although this simplification was helpful to predict the stress distribution against the wall, the stress distribution inside the failure wedge remained unknown. Khosravi et al. [24] improved the existing formulations by applying a two-dimensional system of equilibrium to derive a formulation for estimation of vertical, horizontal and shear stresses at any arbitrary point inside the failure wedge as well as along the retaining wall.

Using experimental and analytical approaches, a large number of studies have been carried out to investigate the lateral earth pressure on retaining wall. However, the main mechanism which controls the behavior of retaining wall is unknown and further studies are required. Numerical modelling provides a low cost and scientific tool to study the effects of different parameters and controlling mechanism without the difficulties in preparation and conducting experiments. Extensive numerical modeling, mostly using Finite Element Method (FEM), have been performed to estimate the lateral earth pressure exerting from the retained soil against the wall [4,5,28-30]. Despite the suitability of FEM for problems of retaining wall, Discrete Element Method (DEM) is confirmed to be a more agreeable alternative approach for simulation of large soil displacements and particle rearrangement near the retaining wall, when large deformations and local soil-structure interactions are considered in modeling [31].

Particle Flow Code (PFC) is a discrete element code in which the material is simulated by an assembly of discrete spherical particles in PFC3D, or circular particles in PFC2D. In this code, the mechanical behavior of material is simulated by the force interaction between particles and displacement of these particles. The inter-particle forces at contact points between particles and Newton’s laws of motion control the basic relationship between forces and particles motions [32]. The particles can be glued together with bonds which is used for simulation of rocks and cohesive soils or can be freely move at contact points which can be employed for simulation of granular (cohesionless) soils and rock muckpiles. This software has been successfully used for simulation of the mechanical behavior of soils [33-34], rocks and jointed rock masses [35-39].

In this paper, a backfilled wall is simulated using PFC2D code and the behavior of a rigid retaining wall under active translation mode is investigated. The gradual redistribution of lateral stress on the retaining wall is studied and the DEM results are compared against the analytical methods.

2. Backfill soil properties

In PFC, three main components are used for mechanical simulation of material; namely particle, wall and bond. The main component is particle which occupies the volume. The second component, wall, provides the boundary condition for sample generation or applying the velocity boundary condition. The third component is bond which is suitable for simulation of rock materials than cohesionless soil materials and can be employed to study the process of crack initiation and propagation of cemented materials.

As this study aims to model the behavior of cohesionless sandy soils, the soil is simulated using assembly of particles with no bond between them. The mechanical behavior of the model is controlled by the normal stiffness $k_n$, shear stiffness $k_s$ and friction coefficient $\mu$ between particles. Therefore, the normal and shear stiffness controls the deformability of soil and the particle friction coefficient controls the strength of soil material. An essential step before conducting the numerical experiments is determining the particles’ micro-parameters. The common method to determine these parameters is the calibration process in which the micro-parameters are determined by trial and error to reproduce the target macro-scale properties [32].

It is well understood that the simulation time is one of the most important and challenging parameters in DEM numerical investigations. In DEM software such as PFC, the simulation time is significantly affected by the number of particles and calculations with the number approaching to the real number of physical particles are not feasible due to computational demand [33]. However, according to Nadakuru and Michalowski [33], even with relatively large particles, the characteristic features of backfilled soil are replicable. A soil with a uniform grain size distribution was used for this study as shown in Fig. 1. The properties of this soil are listed in Table 1.

![Particle size distribution of the modeling soil.](image)

**Table 1.** Characteristic properties of the modeling material.

<table>
<thead>
<tr>
<th>Materials</th>
<th>Properties</th>
</tr>
</thead>
<tbody>
<tr>
<td>Average particle diameter ($D_{so}$)</td>
<td>1.16 mm</td>
</tr>
<tr>
<td>Uniformity coefficient ($C_u$)</td>
<td>1.55</td>
</tr>
<tr>
<td>Specific gravity ($G_s$)</td>
<td>2.65</td>
</tr>
<tr>
<td>Porosity ($\phi$)</td>
<td>0.21</td>
</tr>
<tr>
<td>Cohesion ($c$)</td>
<td>0 kPa</td>
</tr>
<tr>
<td>Internal friction angle ($\phi$)</td>
<td>20.7$^\circ$</td>
</tr>
<tr>
<td>Poisson's ratio ($\nu$)</td>
<td>0.25</td>
</tr>
<tr>
<td>Normal stiffness ($k_n$)</td>
<td>50 MN/m</td>
</tr>
<tr>
<td>Shear stiffness ($k_s$)</td>
<td>50 MN/m</td>
</tr>
</tbody>
</table>

In order to determine the mechanical properties of the particles, biaxial compression tests were carried out on specimens. A rectangular frame with the dimensions of 70 mm by 200 mm was filled up by assembly of randomly placed particles, as shown in Fig. 2(a). To ensure appropriate connections between particles, isotropic stress is applied between particles [32]. The force chains between particles are illustrated in Fig. 2(b). Then, the confining pressure ($\sigma$) was applied to the specimen and the axial stress ($\sigma$) was increased gradually up to the failure. The appeared shear band in the specimen at failure and the force chains between particles at confining pressure of 4 kPa are shown in Fig. 3. The force chains in Fig. 2(b) and Fig. 3(b) are referring to the dark bands, representing the force paths inside the specimen. These chains show the directions where the force are transferring between soil particles.

It can be seen that the shear band inclined at an angle of approximately 55$^\circ$ with the major principal plane. Using the well-known equation of $\beta=\pi/4+\phi/2$, this value of $\beta$ suggests a critical-state internal friction angle of $\phi=20^\circ$ for the modeling material which is in good agreement with calculated values reported in Table 1. From the experimental viewpoint, this value of internal friction angle seems to be too low for a sand with $D_{so}$ of 1.16 mm. However, it should be taken into account that the particles defined in the numerical models are pure circular without interlocking.

Due to the fact that the confining pressure in the retaining wall models are very low (less than 5 kPa), the numerical biaxial tests are conducted under low confining pressures as illustrated in Fig. 4. As it is expected for loose sand under low confining pressures, the stress-strain curves have no clear peak values. In other words, the peak and critical state stress values coincide for this type of soil. It is seen that the soil in these biaxial tests reaches to its critical state at strains as low as 0.0005
to 0.001.

The average unit weight ($\gamma$) of a dry backfill soil with specific gravity of $G_s$ and porosity of $n$ can be estimated from the following equation [33].

$$\gamma = G_s \rho_w g (1 - n)$$ (1)

3. Numerical Model Setup

A 2D box, having the width of 220 mm and height of 400 mm is generated where one side of the box is considered as a rigid retaining wall which can move in the horizontal direction. The surface of the retaining wall is defined to be fully rough with a friction equal to the internal friction of the backfill soil.

The retaining wall was then moved horizontally under a constant rate away from the backfill. The lateral earth pressures against the wall were recorded during the wall movement from at-rest to fully active conditions.

3.1. Backfill soil preparation

It is shown that the vertical pressure distribution inside a backfill soil model depends on the method of soil filling [40]. The backfill preparation by air pluviation method can results in a uniform vertical pressure distribution throughout the model [41]. In this method, dry soil is casted into the model chamber in layers with a known constant thickness. The final density of the casted soil will be a function of falling height and flow rate. The used method in this study is illustrated in Fig. 5. The box was filled with layer by layer soil up to a specific thickness were the soil particles dropped under the gravity force. Numerical models with different backfill soil heights of 200 mm, 250 mm and 300 mm are generated as shown in Fig. 5.

3.2. Earth pressure measurement techniques

The earth pressure on the retaining wall can be measured through measuring particles which are in contact with the retaining wall, as shown in Fig. 6, and recording the applied pressure on these particles during the numerical simulation.
The absolute values of the recorded applied forces on the measuring particles are illustrated in Fig. 7 when the retaining wall is at rest (just after backfilling soil in the box) and under active conditions with some horizontal wall movements of 1 mm and 2 mm.

It can be clearly seen that the reaction forces recorded by measuring particles have no rational trend and a random distribution of forces can be observed. This behavior is related to the fact that during preparation of the backfill soil and also during the wall movement under active condition, the measuring particles are not all well-connected to the retaining wall which is due to the random size and also random position of particles. Therefore, measurement of earth pressure using the particles in vicinity of the retaining wall cannot provide acceptable results.

To overcome this problem, segmented measurement walls are used. The rigid retaining wall with the height of 400 mm is divided into 40 segmented rigid walls, each of them has a height of 10 mm as illustrated in Fig. 8. Each of these mini-walls acts as a pressure cell in which the lateral reaction force applied from soil onto these mini-walls are recorded to measure the lateral earth pressure. The average value of lateral earth pressure on each 4 segmented walls are considered as one recording point as indicated in Fig. 8. To observe the influence of soil arching at the lower corner of the retaining wall, the lateral earth pressure on the segmented wall located at the lower corner (PS0) is also recorded individually.

4. Results and Discussions

4.1. At-rest lateral earth pressure

Variation of the lateral earth pressure during backfilling process for a model with the target backfill height of 300 mm is shown in Fig. 9. As the height of backfill soil behind the retaining wall increases, the lateral earth pressure on the segmented walls increases gradually.

The lateral earth pressure distribution against the backfill height is shown in Fig. 10. The lateral earth pressure and backfill height in Fig. 9 and Fig. 10 are normalized by \( \gamma H \) and \( H \) respectively, where \( \gamma \) is the unit weight of the backfill soil and \( H \) is the backfill height.

Fig. 10 demonstrates that using the air pluviation method in simulation of the backfill, results in a nearly linear pressure distribution on the wall except for the lower corner of the wall due to soil arching. These observations are in agreement with experimental results of Khosravi et al. [9] and numerical results of Nadukuru and Michalowski [33].

The value of at-rest earth pressure coefficient \( (K_a) \) and active earth pressure coefficient \( (K_s) \) for a normally consolidated sand can be approximated by the following well-known equations of Jaky [42] and Rankine [21].

\[
K_a = 1 - \sin \phi \tag{2}
\]

\[
K_s = \frac{1 - \sin \phi}{1 + \sin \phi} \tag{3}
\]

Where \( \phi \) represents the internal friction angle of the backfill soil.
The theoretical at-rest earth pressure distribution developed by Jaky [42] is also plotted in Fig 10 for comparison.

It is clear that the local soil arching observed in physical modeling of Khosravi et al. [9] (Fig. 11(a)) is also observed here at the lower corner of the numerical model as shown in Fig. 11(b). This micro phenomenon reduces the at-rest earth pressure at the lower corner of the wall models (see Fig. 10).

Fig. 11. Local soil arching at the lower corner of the model.

4.2. Active lateral earth pressure

Variations of the lateral earth pressure during wall displacement, with a constant displacement rate of 0.002 mm/s, are shown in Fig. 12 for tests with different wall heights. The horizontal axis represents the cumulative wall displacement normalized by the backfill height \( H \) from at-rest condition, and the vertical axis represents the lateral earth pressure normalized by \( \gamma H \) where \( \gamma \) is the unit weight of the backfill soil.

Fig. 12. Changes in lateral earth pressure with wall displacement (Dis represents the wall displacement in millimeters).

The lateral earth pressure changes by wall movement from at-rest condition under a rigid translational mode. This change is very sharp in the movement onset up to the normalized wall movement of 0.0002 to 0.0005. Increment of the wall movement beyond this critical value results the earth pressure reached to a relatively steady state where the backfill soil is reached to a fully active condition. The required normalized wall movement to reach this condition is defined as normalized active wall movement (\( \Delta x_\text{a}/H \)). This range of value for normalized active wall movement is in good agreement with the experimental results of Fang and Ishibashi [3] and numerical results of Chang [5] where both of them measured a similar range of \( \Delta x_\text{a}/H=0.0003-0.0005 \). However, the numerical study of Matsuzawa and Hazarika [6] suggested \( \Delta x_\text{a}/H=0.0005-0.001 \) for the normalized active wall movement.

It should be noted that the values of active wall movement are very close to the values of required strain for the soil to reach its critical state in previously reported biaxial tests.

The numerical values of at-rest earth pressure (corresponding to \( \text{Dis}/H=0.0000 \) in Fig. 12) and fully active earth pressure (corresponding to \( \text{Dis}/H=0.0030 \) in Fig. 12) for all wall models are summarized in Fig. 13. The values of earth pressure and backfill height are normalized by \( \gamma H \) and \( H \), respectively.

The linear distributions for at-rest and active conditions were predicted by Jaky [42] and Rankine [2], respectively, and some non-linear arch-based equations (Handy [20], Paik and Salgado [23] and Khosravi et al. [24]) are also shown in these figures for comparison.

As shown in Fig. 13(a), a good agreement can be found between the numerical results and the analytical model of Jaky [42] conducted at-rest condition at the upper portion of the wall. However, at the lower portion of the wall, Jaky’s equation underestimates the lateral pressure.

At active condition, as shown in Fig. 13(b), linear distribution of Rankine [2] has a relatively good agreement with the numerical data at the upper portion of the wall, however, it overestimates the values at the lower portion. The reason of overestimation is that the Rankine method does not take the soil arching into account. On the other hand, the arch-based equations of Paik and Salgado [23] and Khosravi et al. [24] show relatively good agreement with the numerical data at the lower portion of the wall, but they overestimate the values at the upper portion. The difference in these data at the upper portion may be related to the complete circular shape of simulated soil particles in the software. Technically, the soil particles are not typical circles and their frictional
resistance is not only due to internal friction, but also due to interlocking. Of interlocking between the soil particles will result in a lower internal friction angle for the soil than the expected values. Therefore, it is recommended to use a combination of clumped particles in simulation. The backfill soil reaches to its critical state at a horizontal wall movement almost corresponding to axial strain in biaxial tests conducted on the same soil under equivalent confining pressures. Under at-rest condition, the equation of Jaky [42] properly predicts the numerical results at the upper portion of the wall, butunderestimates the lateral pressure at its lower portion. The phenomenon of arching at the lower corner of the wall results in a reduction in lateral earth pressure on the toe of the wall even under at-rest condition before applying any movement to the wall. Under active condition, liner distribution of Rankine [2] shows a good prediction at the upper portion but overestimates the earth pressure at the lower portion of the wall. On the other hand, predictions from arch-based equations are acceptable only for the lower portion of the wall.

**REFERENCES**


