

Influence of Magnetic Wire Positions on Free Convection of Fe₃O₄-Water Nanofluid in a Square Enclosure Utilizing with MAC Algorithm

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ABSTRACT

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The augment of heat transfer and fluid of buoyancy-driven flow of Fe₃O₄-Water nanofluid in a square cavity under the influence of an external magnetic field is studied numerically. Cold temperature is applied on the side (vertical) walls and high temperature is imposed on the bottom wall while the top wall is kept at thermally insulated. The governing non-dimensional differential equations are solved using Marker and Cell (MAC) Algorithm. The developed MATLAB code is validated with previous literature and it gives good agreement. The effects of Rayleigh number Ra, Prandtl number Pr and Hartmann number Ha on the flow and heat transfer characteristics are analyzed. Results indicate that the temperature gradient is an increasing function of the buoyancy force. The heat transfer characteristics and flow behavior are presented in the form of streamlines and isotherms. The position of magnetic wire is played a vital role in controlling of heat transfer rate.

1. Introduction

Nanotechnology plays an innovative tool for enhancement of heat transfer. Magnetic nanofluids (ferrofluid) are also called smart fluids or functional fluids, which are stable colloidal suspensions of sub-domain magnetic particles (iron, nickel, cobalt, and their oxides such as magnetite) with a particle size of less than 20 nm dispersed in a base fluid such as water, oil, ethylene glycol, etc. The stability of suspension, a monolayer of insoluble surfactant is discussed and reported [1–3]. Magnetic nanofluids are gained much interest in recent years, whereas it has used controlled by external magnetic field (MF) and have received several applications, which includes dynamic sealing, heat dissipation, damping and doping technological materials [4–6]. Most published studies on ferrofluid have focus on enhancing heat transfer by experimental and numerical methods [7–10].

One of the most scientific challenges in the industrial areas is cooling technology. Increasing the rate of cooling by traditional tools (*i.e.* fins and micro channel) has already reached their limits. Nanofluid, an engineered colloidal suspension of nanoparticles in a base fluid, have been applied in several engineering applications, which includes, the photonics, transportation, electronics, and

energy supply industries [11–15] due to its enhanced thermal conductivity and convective heat transfer coefficient compared to the base fluid [16–19]. Heat transfer enhancement through nanofluid in a square cavity is studied numerically, the first person Khanafer *et al.* [20]. They also notice that to increase of nanoparticles volume fractions leads to the rate of nanofluid heat transfer is increased. Jang and Choi [21] investigated thermal characteristics in a rectangular enclosure with water based nanofluid. They are conducted numerical analysis of the rectangular enclosure heated from bottom wall; in addition, they are taken 6 nm copper and 2 nm diamond. Stoian *et al.* [22] study natural convection enhancement through magnetic nanofluid (Fe₃O₄) by experimentally. Aaiza Gul *et al.* [23] conducted comparison study of MHD mixed convection between water with magnetic (Fe₃O₄) ferric oxides nanoparticles non-magnetic (Al₂O₃) aluminium oxides nanoparticles of vertical channel. Nader *et al.* [24] Carried out natural convection study of non-uniform heating of bottom wall (other walls are isothermal cold walls) of square enclosure with different water based nanofluid. Sinusoidal heating of side wall of enclosure-based study of natural convection of water based nanofluid (Fe₃O₄) with joule heating and constant magnetic field is examined by [25]. They are found that the heat transfer improvement rate by the ferrite nanoparticles with base

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fluid. The influence of inclination on natural convection of water-Based nanofluid in a *C shaped enclosure* is study by numerically with constant magnetic field is reported [26]. The similar work is done by Abedini *et al.* [27], this study they are implemented SIMPLE algorithm and studied the natural convection in C-shaped enclosure filled with water based nanofluid (Fe₃O₄) with the influence of baffle and magnetic field. Convective flows and heat transfer analysis in a rectangular enclosure with water –Fe₃O₄ under the affected oval – shaped heat source within the enclose is introduced by Moraveji and Hejazian [28]. They are studied heat transfer characteristics in a water based nanofluid (Fe₃O₄) with different size of oval-shaped heat source.

A ferrofluid acts as a fluid that is influenced by a magnetic wire and externally imposed magnetic fields has been used to control and fluid direct of ferrofluid, due to its numerous applications in science and engineering. Which include, electronic packing, mechanical engineering, thermal engineering, aerospace and bioengineering [29–32]. Sheikholeslami *et al.* [33] examine the impact of external magnetic field on natural convection of water – Fe₃O₄ in an enclosure. Sheikholeslami and Vajravelu [34] performed control volume based finite element method of natural convection of water –Fe₃O₄ in a square enclosure in presence of heat source has constant heat flux on bottom wall and the influence of the variable magnetic source. Sheikholeslami and Ganji [35] simulated the convective flow in an enclosure (shape =1/4 of circle portion) with the impact of variable magnetic field and they are found the effect of radiation becomes stronger for higher buoyancy forces. Sheikholeslami *et al.* [36] analyzed flow and heat transfer in a porous enclosure with same geometry of [35] under the impact of external magnetic field. Combined magnetohydrodynamic and ferrohydrodynamic effects on water – Fe₃O₄ in an enclosure with constant heat flux of inner boundary and constant temperature of out boundary in presence of dipole external magnetic sources has been discussed [37] and the same enclosure with inner circular boundary has constant hot temperature whereas the other walls are isothermal cold temperature with the impact of opposite variable magnetic wires are performed [38]. The flow and heat transfer are examined with the impact of magnetic field and the non-dimensional governing equations are employed by the effect projection scheme in MAC algorithm has been discussed in literature [39-42].

The aim of this simulation is to examine the affected magnetic source on nanofluid hydrothermal treatment in a square enclosure. MAC algorithm is chosen to employ the governing partial non-dimensional equations. The literature survey shows that, the investigation of convection and heat transfer of ferrofluid with base fluid in a square enclosure in presence external magnetic field and spatially varying magnetic wire has been wide range of Rayleigh number and Hartmann number to the best of authors' knowledge has not been studied so far. Effects of Rayleigh and Hartmann numbers, are taken into account to study heat transfer characteristics.

2. Mathematical modelling and Governing equations

A In this paper, the thermally active side walls of the cavity are maintained at uniform cold temperatures are considered while the bottom wall is maintained at high temperature and the other wall is thermally insulated. **Fig.1** reveals the current computational domain of interest with boundary conditions.

To express the magnetic field strength, one can consider that the magnetic source represents a magnetic wire placed vertical to the *x-y* plane at the point (\bar{a}, \bar{b}) . The components of the

magnetic field's intensity $(\overline{H}_x, \overline{H}_y)$ and strength (\overline{H}) can be considered as [45].

$$\overline{H}_x = \frac{\gamma}{2\pi} \frac{1}{(x-\bar{a})^2 + (y-\bar{b})^2} (y-\bar{b}) \quad (1)$$

$$\overline{H}_y = \frac{\gamma}{2\pi} \frac{1}{(x-\bar{a})^2 + (y-\bar{b})^2} (x-\bar{a}) \quad (2)$$

$$\overline{H} = \sqrt{\overline{H}_x^2 + \overline{H}_y^2} = \frac{\gamma}{2\pi} \frac{1}{\sqrt{(x-\bar{a})^2 + (y-\bar{b})^2}} \quad (3)$$

Where γ is the magnetic field's strength at the source (of the wire) and (\bar{a}, \bar{b}) is the position where the source is located. Let us consider the unsteady two-dimensional natural convective laminar flow of fluid in a square cavity with length of side walls equal to *L*. The gravity acts normal to the *x*-axis and a magnetic source is considered by placing a magnetic wire vertically on to the *x y*-plane at the point (\bar{a}, \bar{b}) . In this study the magnetic source is located at e1, e2 and e3 (i.e. **e1**= (0.5 columns, 1.01 rows), **e2** = (0.5 columns, 1.01 rows) and **e3**= (0.5 columns, 1.01 rows)). The thermal Radiation and Joule heating are negligible. The thermo physical properties of the fluid are assumed to be constant except the density variation in the buoyancy force, which is approximated according to the Boussinesq approximation.

Under the above assumptions with the Boussinesq approximation, the governing equations of conservation of mass, momentum and energy equations can be written In the Cartesian coordinate system as follows:

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0 \quad (4)$$

$$\begin{aligned} \frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = & -\frac{1}{\rho_{nf}} \frac{\partial p}{\partial x} + \nu_{nf} \left(\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right) \\ & - \frac{\sigma_{nf}}{\rho_{nf}} \mu_0^2 \left[\overline{H}_y^2 u - \overline{H}_x \overline{H}_y v \right] \end{aligned} \quad (5)$$

$$\begin{aligned} \frac{\partial v}{\partial t} + u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} = & -\frac{1}{\rho_{nf}} \frac{\partial p}{\partial y} + \nu_{nf} \left(\frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} \right) \\ & + \frac{\sigma_{nf}}{\rho_{nf}} \mu_0^2 \left[\overline{H}_x \overline{H}_y u - \overline{H}_x^2 v \right] + g \beta_{nf} (T - T_c) \end{aligned} \quad (6)$$

$$\begin{aligned} \frac{\partial T}{\partial t} + u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} = & \alpha_{nf} \left(\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} \right) \\ & + \frac{\sigma_{nf}}{(\rho c_p)_{nf}} \mu_0^2 \left(\overline{H}_y u - \overline{H}_x v \right)^2 \\ & + \frac{\mu_{nf}}{(\rho c_p)_{nf}} \left\{ 2 \left(\frac{\partial u}{\partial x} \right)^2 + 2 \left(\frac{\partial v}{\partial y} \right)^2 + \left(\frac{\partial v}{\partial x} + \frac{\partial u}{\partial y} \right)^2 \right\} \end{aligned} \quad (7)$$

Where $\mu_{nf} = \frac{1}{(1-\phi)^{2.5}}$

$$\rho_{nf} = \rho_s \phi + (1-\phi) \rho_f$$

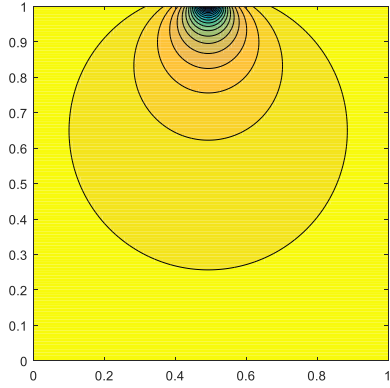
$$\alpha_{nf} = \frac{\kappa_{nf}}{(\rho C_p)_{nf}}$$

$$(\rho C_p)_{nf} = (\rho C_p)_s \phi + (\rho C_p)_f (1-\phi)$$

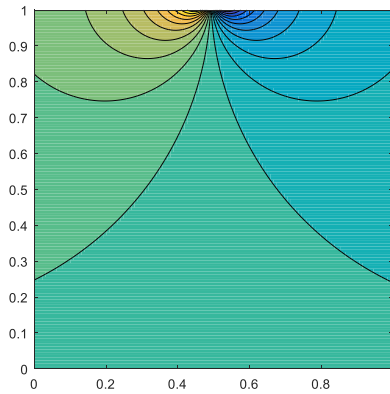
$$\beta_{nf} = \beta_f (1-\phi) + \beta_s \phi$$

$$\kappa_{nf} = \frac{-2\phi(\kappa_f - \kappa_s) + 2\kappa_f + \kappa_s}{\kappa_f \phi(\kappa_f - \kappa_s) + 2\kappa_f + \kappa_s}$$

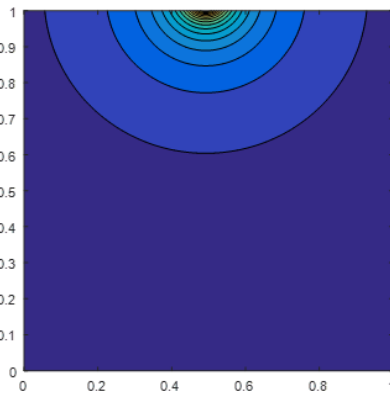
$$\frac{\sigma_{nf}}{\sigma_f} = 1 + \frac{3\left(\frac{\sigma_s}{\sigma_f} - 1\right)\phi}{\left(\frac{\sigma_s}{\sigma_f} + 2\right) - \left(\frac{\sigma_s}{\sigma_f} - 1\right)\phi}$$



(a) $H_x(x,y)$



(b) $H_y(x,y)$



(c) $H(x,y)$

Figure 1. Contours of the (a) magnetic field intensity component in x direction H_x ; (b) magnetic field intensity component in y direction H_y (c) magnetic field strength H .

The following dimensionless variables are introduced:

$$\tau = \frac{tv}{L^2}, X = \frac{x}{L}, Y = \frac{y}{L}, U = \frac{uL}{\nu}, V = \frac{vL}{\nu}$$

$$\theta = \frac{T - T_c}{T_h - T_c}, P = \frac{pL^2}{\rho\nu^2},$$

(8)

$$(H, H_x, H_y) = \left(\frac{\overline{H}, \overline{H}_x, \overline{H}_y}{H_0}, \overline{H}_0 = \overline{H}(a,0) = \frac{\gamma}{2\pi|b|} \right)$$

Using (8), Equations (4) – (7) can be written in dimensionless form as

$$\frac{\partial U}{\partial X} + \frac{\partial V}{\partial Y} = 0 \tag{9}$$

$$\frac{\partial U}{\partial \tau} + U \frac{\partial U}{\partial X} + V \frac{\partial U}{\partial Y} = -\frac{\partial P}{\partial X} \tag{10}$$

$$+ A \text{Pr} \left(\frac{\partial^2 U}{\partial X^2} + \frac{\partial^2 U}{\partial Y^2} \right) - B \delta [H_y^2 U - H_x H_y V]$$

$$\frac{\partial V}{\partial \tau} + U \frac{\partial V}{\partial X} + V \frac{\partial V}{\partial Y} = -\frac{\partial P}{\partial Y} \tag{11}$$

$$+ C \text{Pr} \left(\frac{\partial^2 V}{\partial X^2} + \frac{\partial^2 V}{\partial Y^2} \right) - D \delta [H_x^2 V - H_x H_y U] + E \chi \theta$$

$$\frac{\partial \theta}{\partial \tau} + U \frac{\partial \theta}{\partial X} + V \frac{\partial \theta}{\partial Y} = F \left(\frac{\partial^2 \theta}{\partial X^2} + \frac{\partial^2 \theta}{\partial Y^2} \right)$$

$$+ G \lambda (H_y U - H_x V)^2 \tag{12}$$

$$+ H \times Ec \left\{ 2 \left(\frac{\partial U}{\partial X} \right)^2 + 2 \left(\frac{\partial V}{\partial Y} \right)^2 + \left(\frac{\partial V}{\partial X} + \frac{\partial U}{\partial Y} \right)^2 \right\}$$

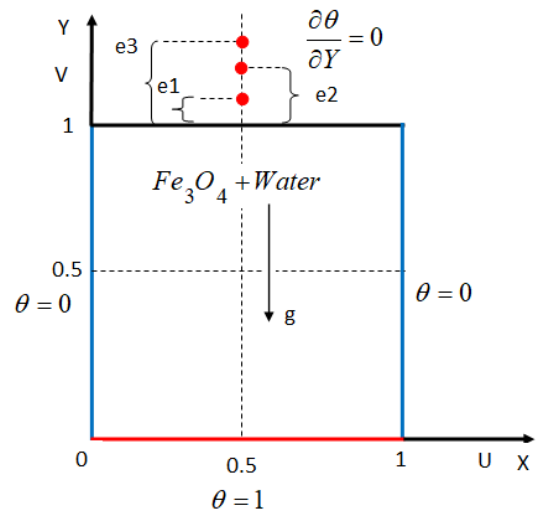


Figure 2. Physical geometry

With dimensionless parameters

$$Ha = L\mu_0 H_0 \sqrt{\frac{\sigma}{\mu}}, Ec = \frac{\nu^2}{c_p \Delta T L^2}, \text{Pr} = \frac{\nu}{\alpha}, \chi = Ra \times \text{Pr},$$

$$Ra = \frac{g\beta(T - T_c)L^3}{\nu\alpha}, \delta = Ha^2 \times \text{Pr}, \lambda = Ha^2 \times Ec,$$

$$A = \frac{\mu_{nf} / \mu_f}{\rho_{nf} / \rho_f} = C, B = \frac{\sigma_{nf} / \sigma_f}{\rho_{nf} / \rho_f} = D, E = \frac{\beta_{nf}}{\beta_f},$$

$$F = \frac{\kappa_{nf} / \kappa_f}{(\rho C_p)_{nf} / (\rho C_p)_f}, G = \frac{\sigma_{nf} / \sigma_f}{(\rho C_p)_{nf} / (\rho C_p)_f},$$

$$H = \frac{\mu_{nf} / \mu_f}{(\rho C_p)_{nf} / (\rho C_p)_f}$$

The appropriate boundary conditions for the present problem are
 On the bottom wall $\theta = 1$
 On the side walls $\theta = 0$
 On the top wall $\frac{\partial \theta}{\partial n} = 0$
 On all walls $U = V = 0$
 The local Nusselt number on the heat source surface can be expressed as

$$Nu = \frac{\kappa_{nf}}{\kappa_f} \left. \frac{\partial \theta}{\partial X} \right|_{Y=0}$$

The average Nusselt number is evaluated by integrating Nu along the heat source

$$\overline{Nu} = \frac{1}{L} \int_0^L Nu dX$$

Flow field of fluid in the present problem is visualized through streamline which is obtained from stream function. Stream function is defined from velocity components U and V . The two-dimensional flow stream function and velocity components Relations are given by,

$$U = \frac{\partial \psi}{\partial Y}, V = -\frac{\partial \psi}{\partial X}$$

Table 1. Thermo physical properties of water and nanoparticles

	$\rho(kg/m^3)$	$C_p(J/kg\ k)$	$\kappa(W/mk)$	$\beta \times 10^5(k^{-1})$	$\sigma(\Omega^{-1}m^{-1})$
Water	997.1	4179	0.613	21	0.05
Fe ₃ O ₄	5200	670	6	1.3	25,000

3. Computational details

3.1. Numerical procedure

The MAC Algorithm has been adopted for the solution of the present specified problem. The coupled highly nonlinear governing equations were converted into weak conservative form in the first step. The staged grid system is used for solving Navier Stokes equation while the central difference scheme is used to solve energy equation. We integrate in time by an incremental step $d\tau$ in each iteration, until the final time 1.0 is reached. Iterative technique is used to solve the resulting equations. The solution process was sustained until the required convergent criterion was full-filled which was $\sum_{i,j} |\Omega_{i,j}^{k+1} - \Omega_{i,j}^k| < 10^{-6}$, the generic variable

Ω stands for U, V, P, θ and k denotes the iteration time levels. In the above inequality the subscripts i, j represents the space coordinates X and Y respectively.

3.2. Code validation

A code validation is performed for checking the reliability of the present code. The present code is compared with the results of D. C. Wan *et al.* [23]. The streamlines and isotherms are compared for $Ra = 10^4$ and $Pr = 0.7$ as shown in **Fig. 3**. From the figure it is evident that the streamlines and isotherms produced by the present code are matched with previously published work by D. C. Wan *et al.* [44]. Also, the Local Nusselt number of hot walls is compared for different values of Gr as shown in **Fig. 4**. The error is very negligible if the Nusselt number is compared. The comparisons reveal an excellent agreement with

the reported studies, and hence the present numerical code is completely reliable.

4. Results and discussions

In this computational study the effect of magnetic wire positions on controlling of magnetohydrodynamics natural convection heat transfer in an enclosure which is heated by uniformly along the bottom wall, cold vertical walls and adiabatic top wall is examined. MAC algorithm is adapted to obtained numerical solution. The square cavity is filled with Fe₃O₄- Water nanofluid (with detail thermal properties of Table. 1). The active key parameters effects such as: Rayleigh number ($Ra=10^3, 10^4$ and 10^5), Hartmann number ($Ha=0-5$) with $Ec=10^{-5}$ and volume fraction of nanoparticles ($\phi = 0 - 0.02$) on fluid flow and heat transfer are investigated when $Pr=6.8$.

The influence of magnetic wire position and Rayleigh number on isotherms and streamlines are presented in **Figs.5-8**. It is reveals from these computational Figs. that the flow cells enhance as the magnetic wire place increases from e1 to e3. Also, it can be observed that the temperature contours move upward. The temperature contours are away from bottom wall when increasing of Ra . In addition, that, by enhancing of Rayleigh number the heat transfer mechanism is shifted from conduction to convection. When the magnetic field is applied on the cavity, the velocity profiles are suppressed owing to the retarding influence of the Lorenz force. Thus, augmentation of convection is suppressed significantly. The core vortex cell is moves downwards vertically when the magnetic wire is varying to e3 to e1 positions. The thermal plume intensity is enhanced when increasing of Rayleigh number and magnetic wire position. For this reason, the cluster temperature contours are formed along the cold walls.

The effect of magnetic wire (0.5, 1.05) on velocity profiles for $Ra=10^5, Ha=5, \phi = 0.02$ are presented in the **Fig.9**. Flow behavior within the enclosure is described various sections of the cavity. The U-velocity (**Fig.9a**) along the vertical line from at $X=0.1$ to $X=0.4$ is gradually increased and fall down to at $X=0.5$ and the symmetric nature and opposite velocity is exhibited from $X=0.6$ to $X=0.9$. The V-velocity (**Fig.9b**) along the horizontal line from $Y=0.1$ to $Y=0.9$ is reveals that the increasing nature is shown from $Y=0.1$ to $Y=0.5$ and decreasing function from $Y=0.5$ to $Y=0.9$. In the middle of the enclosure, the velocity is more compare to other positions, due to the uniform heating of bottom wall the fluid rise up in middle part and fall down to cold walls.

The impact of magnetic wire (0.5, 1.05) on velocity profiles for $Ra=10^5, Ha=5, \phi = 0.02$ are shown in the **Fig.10**. Fluid flow velocity variations within the enclosure are presented different sections of the cavity. The U-velocity (**Fig.10a**) along the vertical line from at $X=0.1$ to $X=0.4$ is gradually increased and at $X=0.5$ the fluid velocity is constant up to $Y=0.8$ while the fluid velocity raises and decreases to zero. The symmetric nature and opposite velocity are exhibited from $X=0.6$ to $X=0.9$. The V-velocity (**Fig.10b**) along the horizontal line from $Y=0.1$ to $Y=0.9$ is reveals that the increasing profile of V is shown from $Y=0.1$ to $Y=0.5$ and decreasing profile of V from $Y=0.5$ to $Y=0.9$. In the middle of the enclosure, the velocity is more compare while this higher velocity place at $X=0.5$ shifted to $X=0.4$ near the magnetic wire, due to the higher impact of magnetic strength.

The variations of local Nusselt number by the impact of magnetic wire positions, Hartmann number and Rayleigh number are illustrating the **Figs.11-13** for fixed $\phi = 0.02$. The heat enhancement is controlled by varying of magnetic wire is presented in **Fig.11**. The magnetic wire is varying from e1 to e5

for $Ra=10^5$, $Ha=5$, $\phi = 0.02$ which leads to increasing the local Nusselt number. The temperature distribution bottom wall is symmetric about $X=0.5$, higher temperature is observed at ends of the hot wall and minimum at middle of the bottom wall. When we expect, the heat transfer rate is reduced with increasing of Hartmann number Ha for $Ra=10^5$, $\phi = 0.02$, positions of Magnetic wire (0.5,1.01). the clear pictorial representation is seen in **Fig.12**. The local Nusselt number gradually increased when increasing of Rayleigh number with $Ha=5$, $\phi = 0.02$ due to the buoyancy effect is enhanced then gradually increasing of fluid flow velocity (it is observed in **Fig.13**).

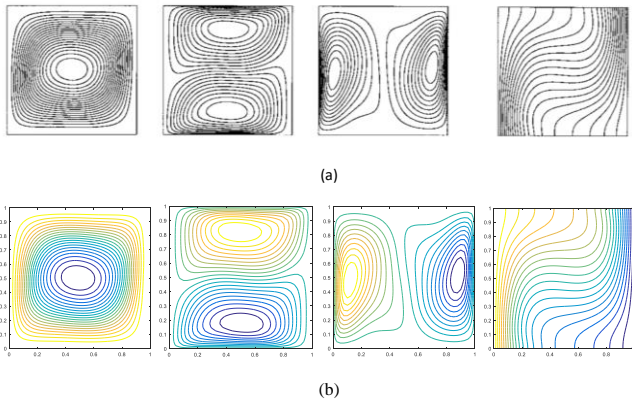


Figure 3. Code validation study, comparison of streamlines u -velocity, v -velocity and isotherms with D. C. Wan *et al.* [15] $Ra=10^4$ and $Pr=0.7$. (a) D. C. Wan *et al.* [44], (b) Present solver (MAC)

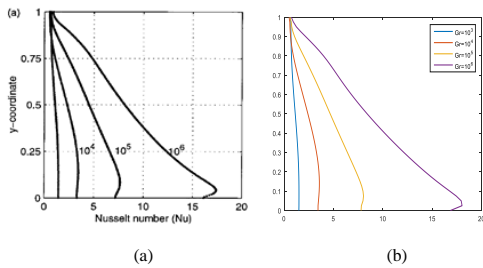


Figure 4. Comparison of Local Nusselt number variation of hot wall for $10^3 < Gr < 10^6$ (a) D. C. Wan *et al.* [44], (b) Present solver (MAC)

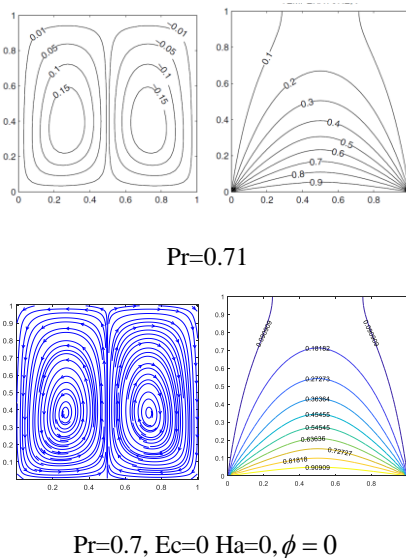


Figure 5. Streamlines and isotherms for bottom wall heating with $Ra=10^3$ and various values of Prandtl number, top row results of Basak *et al.* [43] and bottom row results are nanofluid

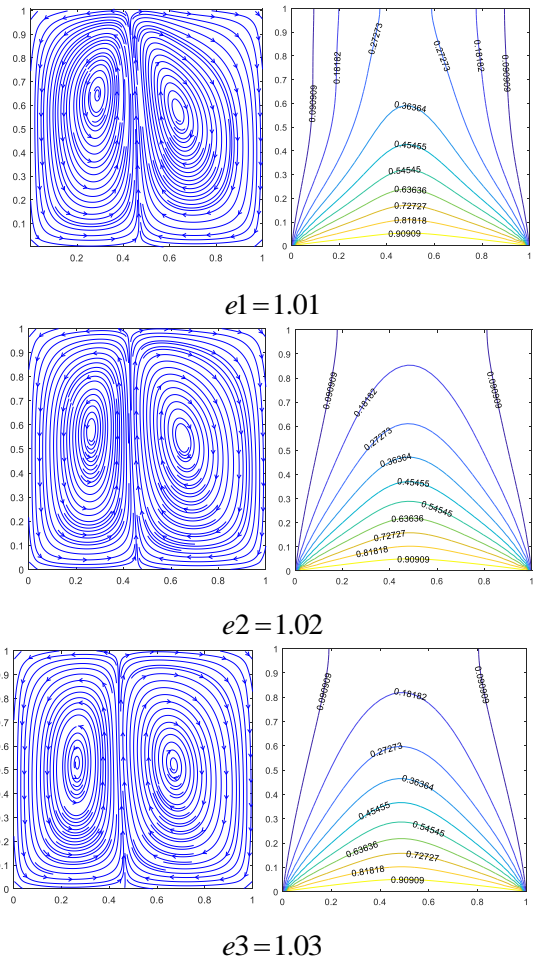


Figure 6. The effect of magnetic wire positions on streamlines (left) and isotherms (right) when $Ra=10^3$, $Ha=5$, $\phi = 0.02$

Pr=0.7, Ec=0 Ha=0, $\phi = 0$

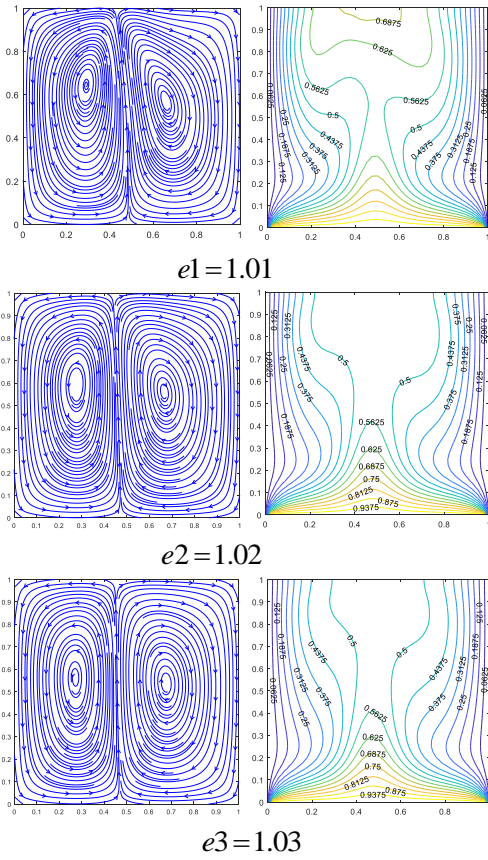


Figure 7. The effect of magnetic wire positions on streamlines (left) and isotherms (right) when $Ra=10^4$, $Ha=5$, $\phi = 0.02$

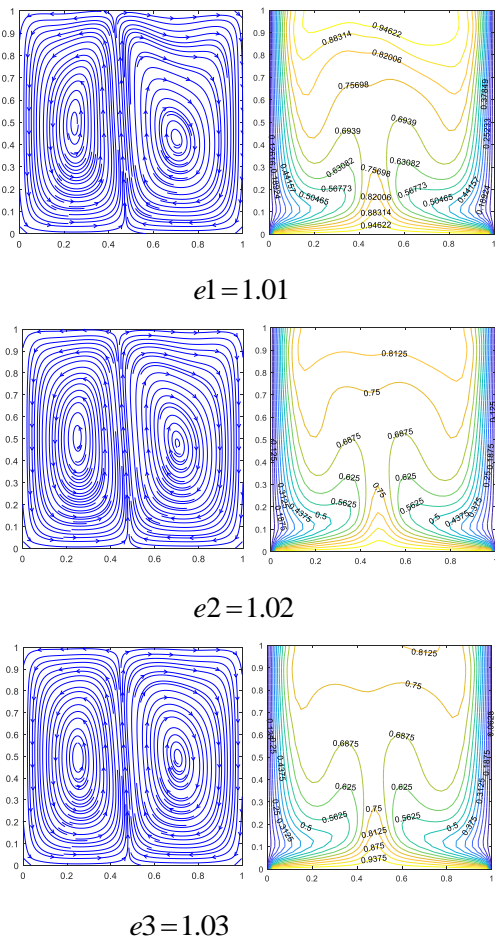


Figure 8. The effect of magnetic wire positions on streamlines (left) and isotherms (right) when $Ra=10^5$, $Ha=5$, $\phi = 0.02$

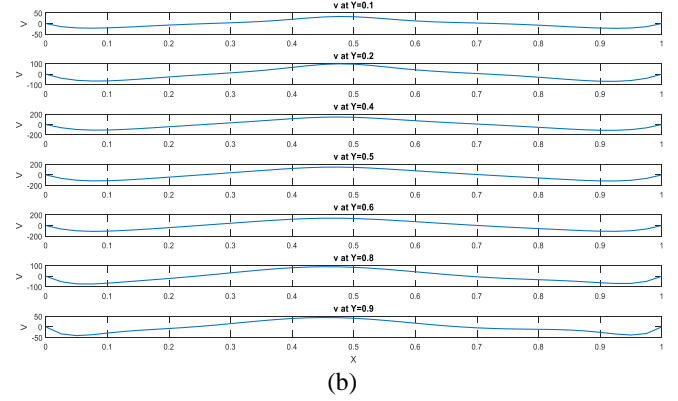
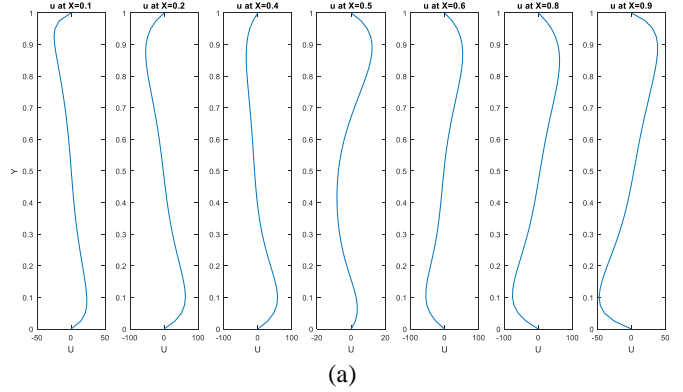


Figure 9. The velocity profile U-(a), V-(b) for various section with $Ra=10^5$, $Ha=5$, $\phi = 0.02$ and magnetic wire position (0.5, 1.05).

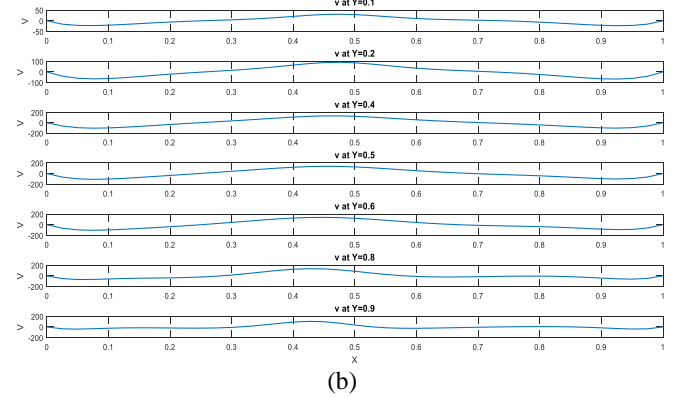
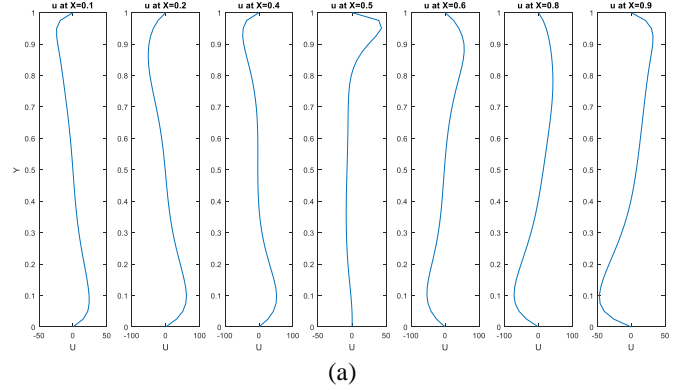


Figure 10. Velocity profile U-(a), V-(b) for various section with $Ra=10^5$, $Ha=5$, $\phi = 0.02$ and magnetic wire position (0.5, 1.01)

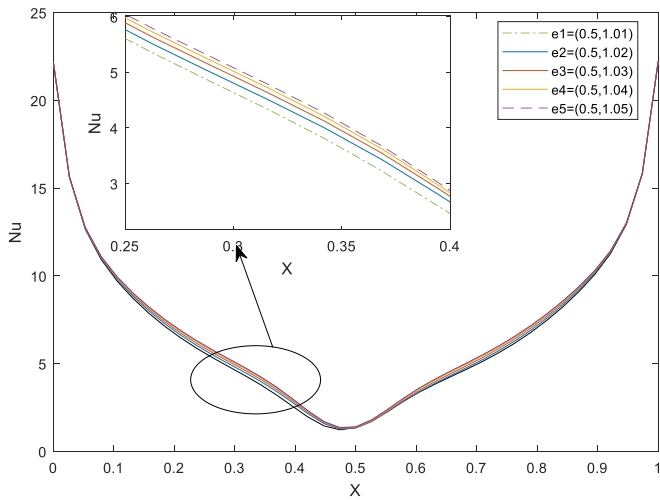


Figure 11. Local Nusselt number along the hot wall with $Ra=10^5$, $Ha=5$, $\phi = 0.02$ and various positions of Magnetic wire.

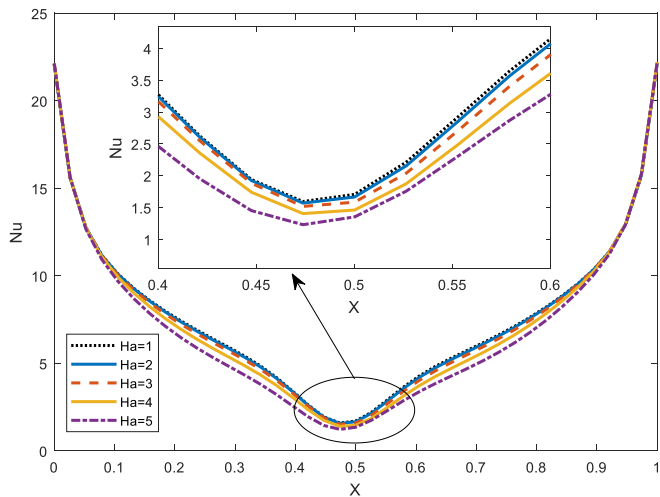


Figure 12. Local Nusselt number along the hot wall with $Ra=10^5$, $\phi = 0.02$, positions of Magnetic wire (0.5,1.01) and various values of Ha .

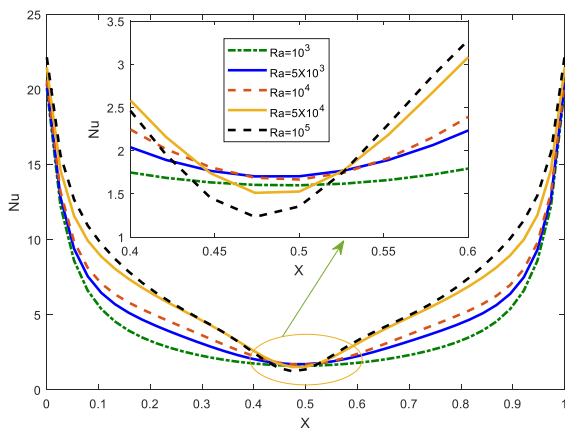


Figure 13. Local Nusselt number along the hot wall with $Ha=5$, $\phi = 0.02$, positions of Magnetic wire (0.5,1.01) and various values of Ra .

5. Conclusions

In this paper the impact of magnetic wire on nanofluid (Fe_3O_4 -water) flow in an enclosure with isothermal temperature boundary conditions and adiabatic to wall has been studied with MAC algorithm. This numerical analysis is performed for pertinent key parameters in the following ranges: Rayleigh number 10^3 - 10^5 , Hartmann number 0-5, the volume fraction is $\phi = 0.02$ and the fixed Prandtl number 6.8 where the positions of magnetic wire is from e1-e5. The study was carried out for various mentioned governing parameters and the results indicates that, Augmentation of heat transfer reduces with an increasing of Hartman number while at the same time heat transfer is increases when increasing of magnetic wire positions. The increase in Hartmann number reduces the both the velocity profiles (U and V components). The increase in Rayleigh number and magnetic wire positions which leads to enhance the local Nusselt number then it is a decreasing function of Ha .

Nomenclature

- C_p Specific heat cavity
- B Constant applied Magnetic field
- $\overline{H_x}$ Magnetic field Intensity in X-direction
- $\overline{H_y}$ Magnetic field Intensity in Y-direction
- \overline{H} Magnetic field strength
- L Length of the cavity
- K Thermal conductivity, ($W m^{-1}k^{-1}$)
- T Temperature, (K)
- u, v Velocity components, ($m s^{-1}$)
- U, V Dimensionless velocity components
- X, Y Dimensionless Cartesian co-ordinates, (m)
- Ec Eckert Number
- Gr Grashof number
- Pr Prandtl Number
- Ha Hartmann number
- Nu Nusselt number
- Ra Rayleigh Number

Greek Symbols

- λ Thermal relaxation parameter
- τ Dimensionless time
- g Gravitational acceleration
- ψ Stream function
- η Efficiency
- ϕ Nano particle volume fraction
- ρ Fluid density, ($kg m^{-3}$)
- α Thermal Diffusivity, ($m^2 s^{-1}$)
- β Thermal Expansion co-efficient
- ν Kinematic Viscosity
- σ Electrical conductivity function

Sub Scripts

- nf Nano Fluid
- f Base Fluid
- s Solid Particle

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