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$$\varepsilon_{ij} = b_{ijkl} \varepsilon_{ijkl}$$

$$\Omega$$

$$\Gamma \equiv \partial\Omega$$

$$\Gamma_d \quad \Gamma_t$$

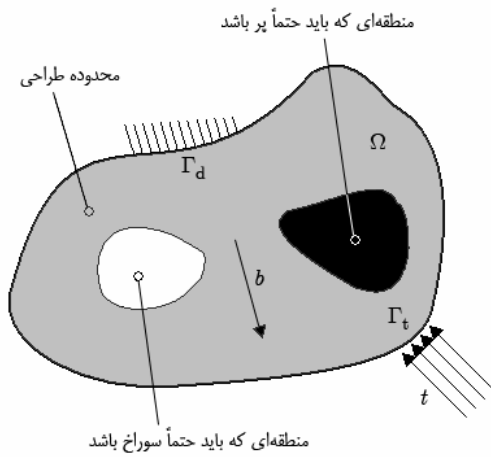
$$\Gamma_t \quad \Gamma_d$$

$$u_d(\mathbf{w})$$

$$(\quad)$$

$$\Omega^d \subset \Omega$$

Matlab



$$\mathbf{w} = (w_1, w_2)$$

$$: [ \quad ]$$

$$\min_{x(\mathbf{w}), u(\mathbf{w})} f(x, u)$$

$$\text{s.t. } a_x(u, v) = l(u), \quad \forall v \in U$$

$$g_i(x) \leq 0, \quad i = 1, \dots, m$$

$$x(\mathbf{w}) \in \{0, 1\}, \quad \forall \mathbf{w} \in \Omega^d$$

$$(\quad)$$

$$(\quad) \quad (\quad)$$

$$a_x(u, v) = l(u), \quad \forall v \in U$$

$$u(\mathbf{w}) \quad x(\mathbf{w})$$

$$U$$

$$f$$

$$g_i$$

$$\Omega^d$$

$$a_x(u, v) \quad l(u)$$

$$: [ \quad ]$$

$$(\quad)$$

$$: [ \quad ]$$

$$E_{ijkl}(x) = x(\mathbf{w}) E_{ijkl}^0$$

$$l(u) = \int_{\Omega} bu \, d\Omega + \int_{\Gamma_t} tu \, ds,$$

$$(\quad)$$

$$E^0$$

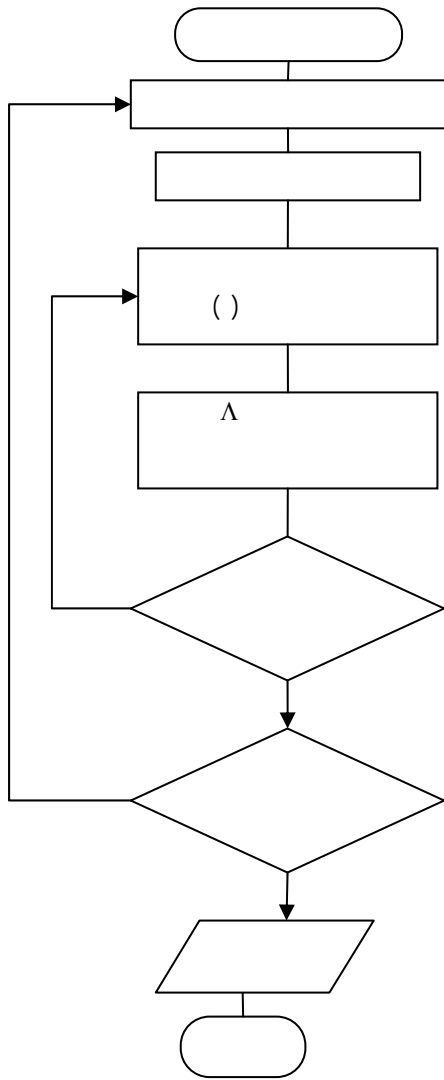
$$(\quad)$$

$$a_x(u, v) = \int_{\Omega} E_{ijkl}(x) \varepsilon_{ij}(u) \varepsilon_{kl}(v) d\Omega.$$

$$(\quad)$$



$$x_e^{k+1} = \begin{cases} \max\{(1-\zeta)x_e^k, \underline{x}\} & \text{if } x_e^k (B_e^k)^\eta \leq \max\{(1-\zeta)x_e^k, \underline{x}\} \\ \min\{(1+\zeta)x_e^k, 1\} & \text{if } \min\{(1+\zeta)x_e^k, 1\} \leq x_e^k (B_e^k)^\eta \\ x_e^k (B_e^k)^\eta & \text{otherwise} \end{cases} \quad (1)$$



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$$0 \leq x \leq 1 \quad [ ]$$

$$0 < \underline{x} \leq x \leq 1 \quad [ ] \quad (2)$$

$$\min_{\mathbf{x}, \mathbf{u}} l(\mathbf{u}) = \mathbf{t}\mathbf{u},$$

$$\text{s.t. } \mathbf{K}(\mathbf{x})\mathbf{u} = \mathbf{f},$$

$$V(\mathbf{x}) = \sum_{e=1}^n x_e v_e \leq V_0,$$

$$0 < \underline{x} \leq x_e \leq 1, \quad e=1, \dots, n \quad (3)$$

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:[ ]  $B_e^k$

$$B_e^k = - \left( \frac{\partial l}{\partial x_e} \right)^k / \Lambda^k v_e, \quad e=1, \dots, n$$

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$\Lambda$

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$$\frac{\partial l}{\partial x_e} = - p x_e^{p-1} \mathbf{u}_e^T \mathbf{K}_e \mathbf{u}_e, \quad e=1, \dots, n$$

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[ - ]  $V=V_0$

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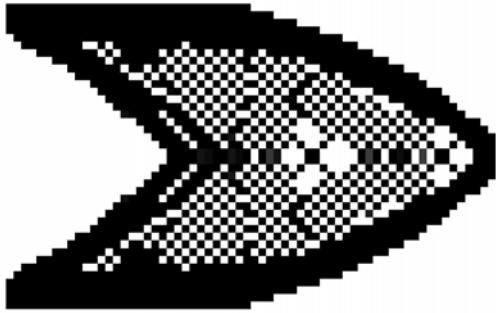
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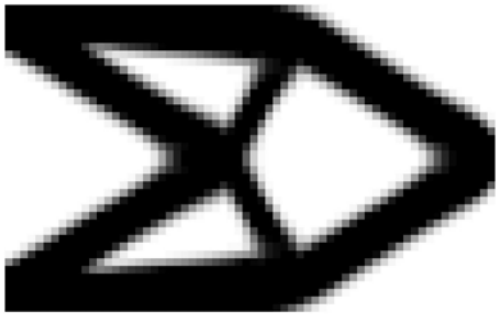
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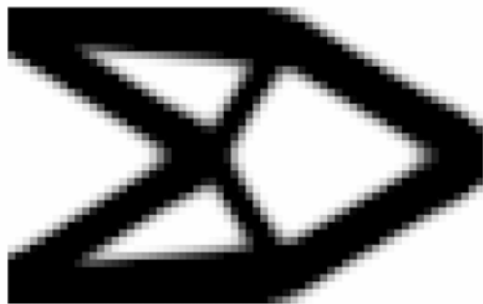
$$\begin{aligned}
 & \hat{\boldsymbol{\varepsilon}}_e \quad \hat{\boldsymbol{\sigma}}_e \\
 ( ) & \quad \cdot \quad \cdot \\
 & : \\
 \frac{\partial l}{\partial x_e} = -\frac{p \cdot \hat{l}_e}{x_e} & \quad \text{SIMP} \\
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 ( ) & \quad \cdot \\
 ( ) & \quad \text{SIMP} \quad \cdot \quad \text{SIMP} \\
 & \quad : \\
 \boldsymbol{\sigma}_e = \mathbf{D}_e \boldsymbol{\varepsilon}_e, \quad \mathbf{D}_e = x_e^p \mathbf{D}^0 & \quad ( ) \\
 i) i & \quad ( ) \\
 s_i^e \quad e & \quad ( \quad \mathbf{D}^0 \\
 & \quad \boldsymbol{\varepsilon}_e \quad \boldsymbol{\sigma}_e \quad (x=1) \\
 \hat{s}_j = \frac{\sum_{k \in W_j} s_{LN(j,k)}^k}{\|W_j\|} & \quad : \\
 ( ) & \quad \hat{s}_j \\
 j & \quad LN(j,k) \quad j \\
 W_j & \quad \cdot \quad k \\
 j & \quad W_j \quad \|W_j\| \\
 & \quad \boldsymbol{\sigma}_e^0 \quad l_e \quad \cdot \quad e \quad \Omega_e \\
 & \quad : \\
 \boldsymbol{\sigma}_e^0 = \mathbf{D}^0 \boldsymbol{\varepsilon}_e, \quad l_e = x_e^p \int_{\Omega_e} \boldsymbol{\varepsilon}_e^T \boldsymbol{\sigma}_e^0 d\Omega & \quad ( ) \\
 & \quad : \quad ( ) \\
 \frac{\partial l}{\partial x_e} = \frac{\partial l_e}{\partial x_e} = -p x_e^{p-1} \int_{\Omega_e} \boldsymbol{\varepsilon}_e^T \boldsymbol{\sigma}_e^0 d\Omega & \quad ( ) \\
 E=1.0 & \quad \cdot \\
 t=1.0 & \quad ( ) \quad ( ) \\
 & \quad : \\
 ( ) & \quad \cdot \quad ( ) \\
 [ ] & \quad \hat{l}_e = \int_{\Omega_e} \hat{\boldsymbol{\varepsilon}}_e^T \hat{\boldsymbol{\sigma}}_e d\Omega \\
 & \quad ( )
 \end{aligned}$$



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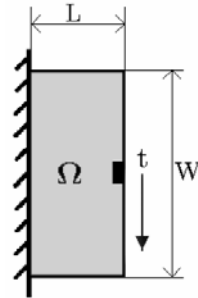
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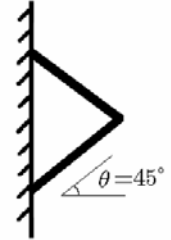
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$$V_0 = 0.2LW$$



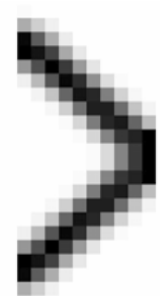
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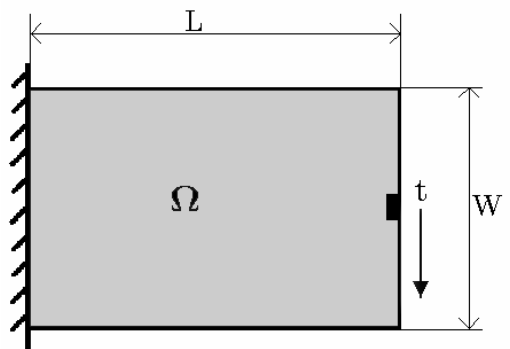
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(L=1.6W)

$V_0=0.5LW$

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$V_0=3L^2$

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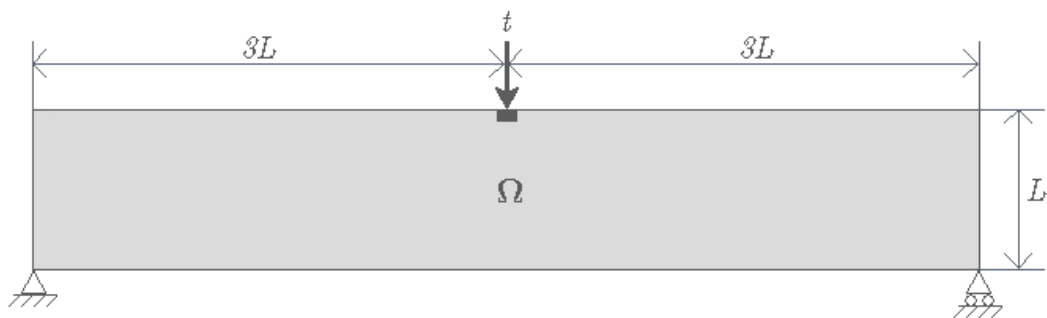
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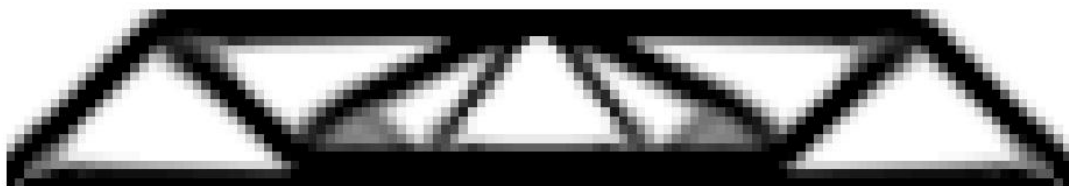
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|---|----------------------------------|
| 1 - Sizing Optimization                         | 19 - Global                      |
| 2 - Shape Optimization                          | 20 - Relaxed Formulation         |
| 3 - Topology Optimization                       | 21 - Mean Compliance             |
| 4 - Integrated Structural Optimization          | 22 - Box Constraints             |
| 5 - Homogenization                              | 23 - Singularity                 |
| 6 - Material Distribution Methods               | 24 - Method of Moving Asymptotes |
| 7 - Remeshing                                   | 25 - Optimality Criteria         |
| 8 - Gray-scale Image                            | 26 - Kuhn-Tucker Conditions      |
| 9 - Solid Isotropic Materials with Penalization | 27 - Damping Factor              |
| 10 - Isotropic                                  |                                  |
| 11 - Design Domain                              |                                  |
| 12 - The Load Linear Form                       |                                  |
| 13 - The Energy Bilinear Form                   |                                  |
| 14 - Weak Form                                  |                                  |
| 15 - Material Model                             |                                  |
| 16 - Mixed                                      |                                  |
| 16 - Closed                                     |                                  |
| 18 - Lack of Continuity                         |                                  |
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